

Residential Construction Site Selection Through Interval-Valued Hesitant Fuzzy CODAS Method

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Abstract. Construction site selection is a complex problem involving many alternatives and conflicting criteria with vague and imprecise evaluations. Fuzzy multi-criteria decision-making methods are the most effective tools to obtain optimum solutions under possibilistic uncertainty. In this paper, a novel interval hesitant fuzzy CODAS method is proposed and applied to a residential construction site selection problem. A comparative analysis with ordinary fuzzy CODAS method is applied for validating the proposed method. Also, a sensitivity analysis is conducted for the stability of the ranking results of the interval hesitant fuzzy CODAS method. The results of the analyses demonstrate the effectiveness of our proposed method.

Key words: construction site, multi-criteria, CODAS, hesitant fuzzy sets, selection problem.

1. Introduction

Selection of the most suitable site for a residential area is one of the conditions determining the quality of living in urban cities. Residential construction site selection problem requires operational, environmental, social, and economic criteria to be considered in the assessment process. These criteria may be intangible, tangible and conflicting with each other. The assessment process is generally realized under vague and imprecise environment, which justifies the usage of the fuzzy set theory.

Residential construction site selection problem can be solved by a multi-criterion decision-making (MCDM) method. MCDM methods help decision-makers to subjectively evaluate the performance of alternatives with respect to the predetermined criteria (Zavadskas *et al.*, 2004, 2014). In the literature, there are many MCDM methods

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such as Analytic Hierarchy Process (AHP) (Saaty, 1980), Technique for Order of Preference by Similarity to Ideal Solution (TOPSIS) (Yoon and Hwang, 1981), ELimination Et Choix Traduisant la REalité (ELECTRE) (Roy, 1991), Analytic Network Process (ANP) (Saaty, 1996), Evaluation Based on Distance from Average Solution (EDAS) (Keshavarz Ghorabae *et al.*, 2015), and Combinative Distance-Based Assessment (CODAS) (Keshavarz Ghorabae *et al.*, 2016). These methods are constructed not only to handle the environmental, human, and social aspects of the problem but also to correctly capture the uncertainties in these aspects. Since residential construction site selection problems involve many uncertainties in terms of vagueness and impreciseness, the best way is to use fuzzy extensions of these MCDM methods.

Fuzzy sets theory was introduced by Zadeh to capture the uncertainties in human thoughts through the degree of memberships of the elements in a set (Zadeh, 1965). In order to increase the capability of handling vagueness and impreciseness in the problems, ordinary fuzzy sets have been extended to many types. Type- n fuzzy sets were developed by Zadeh to reduce the uncertainty of the membership functions in the ordinary fuzzy sets (Zadeh, 1975). Interval-valued fuzzy sets were introduced independently by Zadeh (1975), Grattan-Guinness (1975), Sambuc (1975), Jahn (1975). Intuitionistic fuzzy sets were introduced by Atanassov to show how the hesitancy degree of a decision maker can be handled (Atanassov, 1986). Smarandache developed neutrosophic sets for demonstrating the differences between relativity and absoluteness in the decision makers' preferences (Smarandache, 2005). Hesitant fuzzy sets (HFSs) initially described by Torra (2010) are the extensions of ordinary fuzzy sets where a set of values are possible for the membership of a single element (Torra, 2010). Classical MCDM methods have been extended to their fuzzy versions using these types of fuzzy sets: intuitionistic fuzzy EDAS (Kahraman *et al.*, 2017), ordinary fuzzy CODAS (Keshavarz Ghorabae *et al.*, 2017), type-2 fuzzy AHP (Kahraman *et al.*, 2014), hesitant TOPSIS (Xu and Zhang, 2013), neutrosophic ELECTRE III. In the literature, setting linguistic scale is essentially realized in two ways: the studies using a constant linguistic scale as in Kwong and Bai (2003), Kulak and Kahraman (2005) and the studies using tools such as mathematical programming or statistical modelling to determine the intervals corresponding to the linguistic terms as reviewing in Liao *et al.* (2018) and applied in Cabrerizo *et al.* (2017). Since our paper falls in the studies using a constant linguistic scale, we developed linguistic scales corresponding to fuzzy numbers for our paper.

CODAS is a distance based MCDM method proposed by Keshavarz Ghorabae *et al.* (2016). In this method, the overall performance of an alternative is measured by the Euclidean and Taxicab distances from the negative-ideal point. The CODAS uses the Euclidean distance as the primary measure of assessment. If the Euclidean distances of two alternatives are very close to each other, the Hamming distance is used to compare them. The degree of closeness of Euclidean distances is set by a threshold parameter (Keshavarz Ghorabae *et al.*, 2016). It is quite a new method in the literature but thanks to its advantages it is expected to be used more in the future.

In this paper, a novel hesitant fuzzy CODAS method is developed and applied to the selection of a residential construction site project. The originality of this paper can be

explained by three items. Firstly, we develop a novel fuzzy CODAS method and apply it to a residential construction site selection problem. Secondly, in the proposed method, the weights of the criteria are obtained by hesitant fuzzy AHP method which makes our approach an integrated methodology. Finally, for validating the proposed method, we compare our results with the results of ordinary fuzzy CODAS method. An explanatory sensitivity analysis is also performed to demonstrate the stability of the ranking results of the hesitant fuzzy CODAS method.

The rest of the paper is organized as follows: In Section 2, a literature review on construction site selection problems is given. In Section 3, the steps of ordinary fuzzy CODAS method are presented. In Section 4, the proposed methodology is clarified with its details. In Section 5, the proposed method is applied to a residential construction site selection problem. The paper ends with conclusions and suggestions for further research.

2. Literature Review: Construction Site Selection Problems

Numerous MCDM models have been developed for evaluating construction site location alternatives with respect to the predetermined criteria. We have analysed the studies that can be beneficial for our application and have presented a general evaluation of them. In these studies, MCDM methods are mainly applied for obtaining the solutions of the site selection problems in many different areas.

Cheng *et al.* (2003) studied MCDM methods to support selection of an optimal landfill site and a waste-flow-allocation pattern. Zavadskas *et al.* (2004) applied ELECTRE III method for the selection of the best commercial construction project. It is emphasized that MCDM methods are quite suitable for the evaluation and decision-making assessments for construction projects. Dey and Ramcharan (2008) applied AHP method for the site selection process of expansion on limestone quarry operations to support cement production in Barbados. The results show that AHP is an effective method of decision-making and can consider both objective and subjective factors. Turskis *et al.* (2012) studied the determination of the best construction site alternative for non-hazardous waste incineration plant by using ARAS-F and AHP methods. It can be deducted based on the results that performing more precise assessments is possible with fuzzy sets theory. Balali *et al.* (2012) applied a new algorithm combining ELECTRE III and Preference Ranking Organization Method for Enrich Evaluation II (PROMETHEE II) for decision-making in the construction management processes. Eskandari *et al.* (2012) presented a study of landfill site selection problem by integrating geographic information systems (GIS) and AHP method. Hasanzadeh *et al.* (2013) performed an application of AHP for prioritizing the environmental criteria of coastal oil jetties. The results of the study indicate that ANP findings have a high efficiency for weighting the importance degrees of criteria for environmental construction. Bagocius *et al.* (2014) presented a study about the selection of the most appropriate location for a liquefied natural gas terminal based on the results of different MCDM methods. Results of the study indicate that outcomes of SAW, TOPSIS, and COPRAS methods are consistent and give similar consequences. Zavadskas *et al.*

(2015) applied Weighted Aggregated Sum Product Assessment (WASPAS) method with single-valued neutrosophic sets. The results of the study indicate that applied neutrosophic MCDM method is quite efficient and meets the requirements for the evaluation of intangible factors of the problem. Mousavi *et al.* (2015) investigated the suitability of the Kish Island coastal areas for the establishment of artificial corals reefs using spatial MCDM tool. Results of the study demonstrated that weighted linear combination method should be used for the identification of alternatives and AHP should be used for the prioritization of alternatives. Chaudhary *et al.* (2016) studied fire station suitability zonation mapping of Kathmandu City and determined the best alternative using GIS and AHP methods. Since the results reveal that 13.46% of the considered area is highly suitable for fire station location, zonation map is trustworthy and can be used for the construction of fire stations. Bahrani *et al.* (2016) presented a study on landfill site selection by using fuzzy GIS and ordinary AHP. The authors demonstrated that fuzzy functions for landfill site selection were way better than crisp ones for GIS. Bansal *et al.* (2017) presented a fuzzy decision approach which is a combination of fuzzy synthetic evaluation method and analytic hierarchy process for the selection of most suitable construction method of green buildings. The results show that the proposed model can be an analytical tool to evaluate the applicability of prefabricated or on-site construction methods. Chen *et al.* (2018) studied another construction site location selection problem by applying EDAS and WASPAS methods. They conducted Monte Carlo simulation to check the sensitivity in changes of the criterion weights.

In this paper, we propose a novel hesitant fuzzy CODAS method which provides flexibility to the definition of membership function and to the measurement of distances from negative-ideal solution. In hesitant fuzzy sets, the difficulty in establishing the membership degrees does not arise from a margin of error or a specified possibility distribution of the possible values but arises from our hesitation among a few different values (Zhang, 2013). Thus, the proposed model can make a comprehensive evaluation in terms of both fuzziness and distance measurement, allowing a more accurate representation of knowledge.

3. Ordinary Fuzzy CODAS Method

In this section, preliminaries of ordinary fuzzy sets and steps of ordinary fuzzy CODAS method will be presented.

3.1. Preliminaries: Ordinary Fuzzy Sets

DEFINITION 1. If X is a collection of elements denoted by A , then a fuzzy set \tilde{A} in X is a set of ordered pairs (Zadeh, 1975):

$$\tilde{A} = \{(a, \mu_{\tilde{A}}(a) \mid a \in X)\}, \quad (1)$$

where \tilde{A} in X satisfies the following conditions:

- \tilde{A} is normal,
- \tilde{A} is a closed interval for every $a \in [0, 1]$,
- The support of \tilde{A} must be bounded,
- $\mu_{\tilde{A}}(a)$ is entitled as the membership function of element a which maps to X .

Arithmetic operations of triangular fuzzy numbers are given as follows:

Let $\tilde{A} = (a_1, a_2, a_3)$ and $\tilde{B} = (b_1, b_2, b_3)$ be positive TFNs. Then,

- $\tilde{A} \oplus \tilde{B} = (a_1 + b_1, a_2 + b_2, a_3 + b_3)$,
- $\tilde{A} \ominus \tilde{B} = (a_1 - b_3, a_2 - b_2, a_3 - b_1)$,
- $\tilde{A} \otimes \tilde{B} = (a_1 b_1, a_2 b_2, a_3 b_3)$,
- $\tilde{A} \oslash \tilde{B} = (a_1 \div b_3, a_2 \div b_2, a_3 \div b_1)$.

DEFINITION 2. Let $\tilde{x} = (a, b, c, d)$ be a trapezoidal ordinary fuzzy number. Defuzzification function of this fuzzy number is given as follows (Wang *et al.*, 2006):

$$\tilde{h}(\tilde{x}) = \frac{1}{3} \left((a + b + c + d) - \frac{cd - ab}{(c + d) - (a + b)} \right). \tag{2}$$

DEFINITION 3. Let $\tilde{x} = (a_1, b_1, c_1, d_1)$ and $\tilde{y} = (a_2, b_2, c_2, d_2)$ be the trapezoidal fuzzy numbers. The weighted Euclidean (d_E) and weighted Hamming (d_H) distances between these two fuzzy numbers are defined as follows, respectively:

$$d_E(\tilde{x}, \tilde{y}) = \sqrt{\frac{(a_1 - a_2)^2 + 2(b_1 - b_2)^2 + 2(c_1 - c_2)^2 + (d_1 - d_2)^2}{6}}, \tag{3}$$

$$d_H(\tilde{x}, \tilde{y}) = \frac{|a_1 - a_2| + |b_1 - b_2| + |c_1 - c_2| + |d_1 - d_2|}{6}. \tag{4}$$

3.2. Steps of the Ordinary Fuzzy CODAS Method

The steps of the ordinary fuzzy CODAS method are given as below:

Step 1. Construct the fuzzy decision-making matrix (\tilde{X}_l) of each decision maker and compute the average fuzzy decision matrix (\tilde{X}):

$$\tilde{X}_l [\tilde{x}_{ijl}]_{n \times m} = \begin{bmatrix} \tilde{x}_{11l} & \cdots & \tilde{x}_{1ml} \\ \vdots & \ddots & \vdots \\ \tilde{x}_{n1l} & \cdots & \tilde{x}_{nml} \end{bmatrix}, \tag{5}$$

$$\tilde{X} [\tilde{x}_{ij}]_{n \times m} = \begin{bmatrix} \tilde{x}_{11} & \cdots & \tilde{x}_{1m} \\ \vdots & \ddots & \vdots \\ \tilde{x}_{n1} & \cdots & \tilde{x}_{nm} \end{bmatrix}, \tag{6}$$

$$\tilde{x}_{ij} = \frac{\bigoplus_{l=1}^q \tilde{x}_{ijl}}{q}, \tag{7}$$

where \tilde{x}_{ijl} denotes the fuzzy evaluation score of i th ($i \in \{1, 2, \dots, n\}$) alternative with respect to j th criterion ($j \in \{1, 2, \dots, m\}$) and l th ($l \in \{1, 2, \dots, q\}$) decision maker, and \tilde{x}_{ij} shows the average fuzzy score of i th alternative with respect to j th criterion.

Step 2. Obtain the fuzzy weight of each criterion (\tilde{w}_j) from each decision maker:

$$\tilde{W}_l = [\tilde{w}_{jl}]_{1 \times m}, \quad (8)$$

$$\tilde{W} = [\tilde{w}_j]_{1 \times m}, \quad (9)$$

$$\tilde{w}_j = \frac{\bigoplus_{l=1}^q \tilde{x}_{jl}}{q}, \quad (10)$$

where \tilde{w}_{jl} denotes the fuzzy weight of j th criterion ($j \in \{1, 2, \dots, m\}$) with respect to l th decision maker ($l \in \{1, 2, \dots, q\}$), and \tilde{w}_j shows the average fuzzy weight of j th criterion.

Step 3. Determine fuzzy normalized decision matrix \tilde{N} :

$$\tilde{N} = [\tilde{n}_{ij}]_{n \times m}, \quad (11)$$

$$\tilde{n}_{ij} = \begin{cases} \frac{\tilde{x}_{ij}}{\max_i \mathfrak{S}(\tilde{x}_{ij})} & \text{if } j \in B, \\ 1 - \frac{\tilde{x}_{ij}}{\max_i \mathfrak{S}(\tilde{x}_{ij})} & \text{if } j \in C, \end{cases} \quad (12)$$

where B and C represent the sets of benefit and cost criteria, respectively, and \tilde{n}_{ij} denotes the normalized fuzzy scores and $\mathfrak{S}(\tilde{x}_{ij})$ is calculated by Eq. (2).

Step 4. Calculate the fuzzy weighted normalized decision matrix (\tilde{R}):

$$\tilde{R} = [\tilde{r}_{ij}]_{n \times m}, \quad (13)$$

$$\tilde{r}_{ij} = \tilde{w}_j \otimes \tilde{n}_{ij}, \quad (14)$$

where \tilde{w}_j denotes the fuzzy weight of j th criterion, and $0 < \mathfrak{S}(\tilde{w}_j) < 1$.

Step 5. Determine the fuzzy negative ideal solution ($\tilde{N}\tilde{S}$):

$$\tilde{N}\tilde{S} = [\tilde{n}\tilde{s}_j]_{1 \times m}, \quad (15)$$

$$\tilde{n}\tilde{s}_j = \min_i \tilde{r}_{ij}, \quad (16)$$

where $\min_i \tilde{r}_{ij} = \{\tilde{r}_{ij} \mid \mathfrak{S}(\tilde{r}_{ij}) = \min_i (\mathfrak{S}(\tilde{r}_{ij}))\}$, $k \in \{1, 2, \dots, n\}$.

Step 6. Calculate the weighted Euclidean Distance (ED_i) and weighted Hamming Distance HD_i of alternatives from the fuzzy negative ideal solution as given by Eqs. (3)

and (4):

$$ED_i = \sum_{j=1}^m d_E(\tilde{r}_{ij}, \tilde{ns}_j), \tag{17}$$

$$HD_i = \sum_{j=1}^m d_D(\tilde{r}_{ij}, \tilde{ns}_j). \tag{18}$$

Step 7. Determine the relative assessment matrix (RA):

$$RA = [p_{ik}]_{n \times n}, \tag{19}$$

$$p_{ik} = (ED_i - ED_k) + (t(ED_i - ED_k)(HD_i - HD_k)), \tag{20}$$

where $k \in \{1, 2, \dots, n\}$ and t is a threshold function that is defined as follows:

$$t(x) = \begin{cases} 1 & \text{if } |x| \geq \theta, \\ 0 & \text{if } |x| < \theta. \end{cases} \tag{21}$$

The threshold parameter (θ) of this function can be set by decision maker. In this study, we used $\theta = 0.02$ in our calculations by considering the proposed method and the one proposed bydel Moral *et al.* (2018) which presents how the use of different aggregation operators affects the level of consensus.

Step 8. Calculate the assessment score (AS_i) of each alternative:

$$AS_i = \sum_{k=1}^n p_{ik}. \tag{22}$$

Step 9. Rank the alternatives according to the decreasing values of assessment scores and select the alternative with the maximum assessment score.

4. A Novel Hesitant Fuzzy CODAS Method

In this section, we firstly give basic definitions and operations on hesitant fuzzy sets and then present the steps of our proposed hesitant fuzzy CODAS method.

4.1. Preliminaries: Hesitant Fuzzy Sets

Hesitant fuzzy sets (HFS), initially developed by Torra (2010) are the extensions of regular fuzzy sets which handle the situations where a set of values are possible for the membership of a single element (Rodriguez *et al.*, 2012). Torra (2010) defined hesitant fuzzy sets as follows: let X be a fixed set. A hesitant fuzzy set (HFS) on X is as follows:

$$E = \{ \langle x, h_E(x) \rangle \mid x \in X \},$$

where $h_E(x)$ is a set of some values in $[0, 1]$, denoting the possible membership degrees of the element $x \in X$ to the set E . Xu and Xia (2011a) called $h = h_E(x)$ as a hesitant fuzzy element (HFE).

Some basic definitions about hesitant sets are given in the following (Torra, 2010);

$$\lambda h = U_{\gamma \in h} \{1 - (1 - \gamma)^\lambda\}, \quad (23)$$

$$h_1 \oplus h_2 = U_{\gamma_1 \in h_1, \gamma_2 \in h_2} \{\gamma_1 + \gamma_2 - \gamma_1 \gamma_2\}, \quad (24)$$

$$h_1 \otimes h_2 = U_{\gamma_1 \in h_1, \gamma_2 \in h_2} \{\gamma_1 \gamma_2\}. \quad (25)$$

In the scope of this study, one of the most important operations is finding the distance between two HFEs. The literature provides different approaches for this purpose. Xu and Xia (2011b) defined the hesitant Euclidean distance as in Eq. (26):

$$d_1(h_1, h_2) = \sqrt{\frac{1}{l} \sum_{i=1}^l |h_{1\sigma(i)} - h_{2\sigma(i)}|^2}. \quad (26)$$

Xu and Xia (2011b) proposed Hamming distance measure as in Eq. (27):

$$d_1(h_1, h_2) = \frac{1}{l} \sum_{i=1}^l |h_{1\sigma(i)} - h_{2\sigma(i)}|, \quad (27)$$

where h_1, h_2 are HFEs and l is the number of elements in a HFE, which is called length.

4.2. Steps of HF-CODAS

The steps of the hesitant fuzzy CODAS method are given as below:

Step 1. Construct the initial fuzzy decision matrix \tilde{I} by using Table 1 and the fuzzy decision matrix \tilde{D} :

$$\tilde{I}[\tilde{x}_{ijl}]_{n \times m} = \begin{bmatrix} x_{111}, \dots, x_{113} \dots x_{1m(\tilde{k}-1)}, \dots, x_{1mk} \\ \vdots & & \ddots & & \vdots \\ x_{n11}, \dots, x_{n1l} \dots x_{nm(\tilde{k}-1)}, \dots, x_{nmk} \end{bmatrix}, \quad (28)$$

where x_{ijl} represents the l th ($l = 1, \dots, k$) score value of the i th ($i = 1, \dots, n$) alternative with respect to j th, ($j = 1, \dots, m$) criterion.

Before constructing the fuzzy decision matrix, the maximum number of the membership functions for an alternative is determined as a threshold value in the initial decision matrix (see in Eq. (28)). If any score of an alternative is lower than the threshold value, the smallest membership degree of this alternative is assigned to the same alternative as a new membership degree until the value of membership degree equals the threshold value.

Table 1
Scale for scoring values.

Linguistic terms	Membership function
Unimportant – UI	$[\tau, 1.8]$
Very Poor – VP	$[0.9, 2.7]$
Poor – P	$[1.8, 3.6]$
Medium Poor – MP	$[2.7, 4.5]$
Fair – F	$[3.6, 5.4]$
Medium Good – MG	$[4.5, 6.3]$
Good – G	$[5.4, 7.2]$
Very Good – VG	$[6.3, 8.1]$
Superior – SP	$[7.2, 9]$
τ is a very small number close to 0.	

This procedure is performed for each criterion of each alternative and thus the decision matrix is established as given in Eq. (29).

$$\tilde{D}[\tilde{x}_{ij}]_{n \times m} = \begin{bmatrix} \tilde{x}_{11}^d, \dots, \tilde{x}_{11}^d \dots \tilde{x}_{1m}^d, \dots, \tilde{x}_{1m}^d \\ \vdots \\ \tilde{x}_{n1}^d, \dots, \tilde{x}_{n1}^d \dots \tilde{x}_{nm}^d, \dots, \tilde{x}_{nm}^d \end{bmatrix}. \tag{29}$$

Step 2. Determine fuzzy normalized decision matrix (\tilde{N}):

$$\tilde{N} = [\tilde{x}_{ijl}^{d,n}]_{n \times m}, \tag{30}$$

$$x_{lower\ ij}^{d,n} = \begin{cases} \frac{x_{lower\ ij}^{d,n}}{\max_j \tilde{x}_{ijl}^{d,n}} & \text{if } j \in B, \\ \frac{\min_j \tilde{x}_{ijl}^{d,n}}{x_{upper\ ij}^{d,n}} & \text{if } j \in C, \end{cases} \tag{31}$$

$$x_{upper\ ij}^{d,n} = \begin{cases} \frac{x_{upper\ ij}^{d,n}}{\max_j \tilde{x}_{ijl}^{d,n}} & \text{if } j \in B, \\ \frac{\min_j \tilde{x}_{ijl}^{d,n}}{x_{lower\ ij}^{d,n}} & \text{if } j \in C, \end{cases} \tag{32}$$

where $\tilde{x}_{ijl}^{d,n} = [x_{lower\ ij}^{d,n}, x_{upper\ ij}^{d,n}]$ is a normalized interval valued hesitant fuzzy number in the decision matrix.

Step 3. Calculate the fuzzy weighted normalized decision matrix \tilde{R} :

$$\tilde{R} = [\tilde{r}_{ijl}]_{n \times m}, \tag{33}$$

$$\tilde{r}_{ijl} = \tilde{w}_j \otimes \tilde{x}_{ijl}^{d,n}, \tag{34}$$

where w_j denotes the weight of j th criterion.

Step 4. Determine the fuzzy negative ideal solution \widetilde{NS} :

$$\widetilde{NS} = [\widetilde{ns}_{jl}]_{1 \times m}, \quad (35)$$

$$\widetilde{ns}_j = \min_i \widetilde{r}_{ijl}, \quad (36)$$

where $\min_i \widetilde{r}_{ijl} = \{\widetilde{r}_{ij} \mid \mathfrak{H}(\widetilde{r}_{ijl}) = \min_i(\mathfrak{H}(\widetilde{r}_{ijl}))\}$, $k \in \{1, 2, \dots, n\}$.

Step 5. Calculate the fuzzy weighted Euclidean Distance (ED_i) and fuzzy weighted Hamming Distance (HD_i) of alternatives from the fuzzy negative ideal solution:

$$ED_i = \sum_{j=1}^m d_E(\widetilde{r}_{ijl}, \widetilde{ns}_j), \quad (37)$$

$$HD_i = \sum_{j=1}^m d_D(\widetilde{r}_{ijl}, \widetilde{ns}_j). \quad (38)$$

Step 6. Determine the relative assessment matrix (RA) using Eqs. (19), (20), and (21).

Step 7. Calculate the assessment score (AS_i) of each alternative using Eq. (22).

Step 8. Rank the alternatives according to the decreasing values of assessment scores and select the alternative with maximum assessment score.

The flowchart of the proposed methodology is given in Fig. 1.

5. Application

A council consisting of Metropolitan Municipality Directors, Housing Development Administration and Contractors' representatives would like to determine the location of a residential which has 10,000 residences to be built in the city of Istanbul. The council determined 8 alternative construction sites whose locations are indicated in Fig. 2. The evaluation factors consist of 4 main criteria and 14 sub criteria. The aim is to find the best alternative for the residential construction site based on the pre-determined criteria with respect to the council's opinions. The weights of the criteria are obtained by hesitant fuzzy AHP (Tuysuz and Simsek, 2017). These weights are used in the proposed hesitant fuzzy CODAS to obtain the weighted normalized decision matrix. The results of the integrated methodology are verified with the sensitivity analysis. A comparative analysis is also conducted to show the validation of the proposed method.

5.1. Problem Definition

The contractors agreed to use a scientific method to determine the most appropriate site from the alternate locations in order to obtain the approval of the residential. They formed an academicians' committee composed of 4 people that would carry out the application.

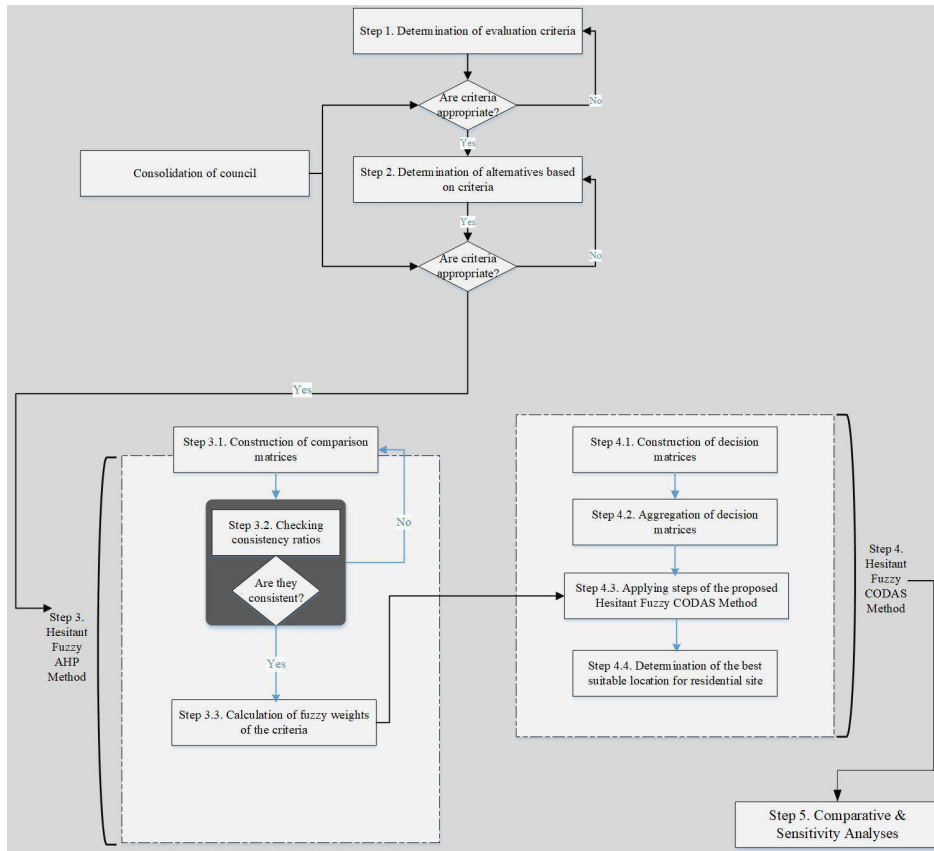


Fig. 1. Flowchart of the application.

Table 2
Determined criteria for the application.

Social Criteria	Attractiveness of land Population characteristics Distance from historical sites Distance from other residential areas	Economic Criteria	Price Infrastructure cost Construction cost Slope of the land
Environmental Criteria	Forestland Agricultural land Human and animal habitats	Technical Criteria	Distance from waste production centers Distance from high-standard roads Distance from industrial areas

Since the problem has too many criteria and alternatives, the committee has decided to use some MCDM methods including our integrated methodology for the solution of this problem. In our integrated methodology, the weights of the criteria are determined by hesitant fuzzy AHP and then, the proposed hesitant fuzzy CODAS method is applied to obtain the best residential construction site. The determined criteria for implementation are given in Table 2.



Fig. 2. Location of alternative residential construction sites.

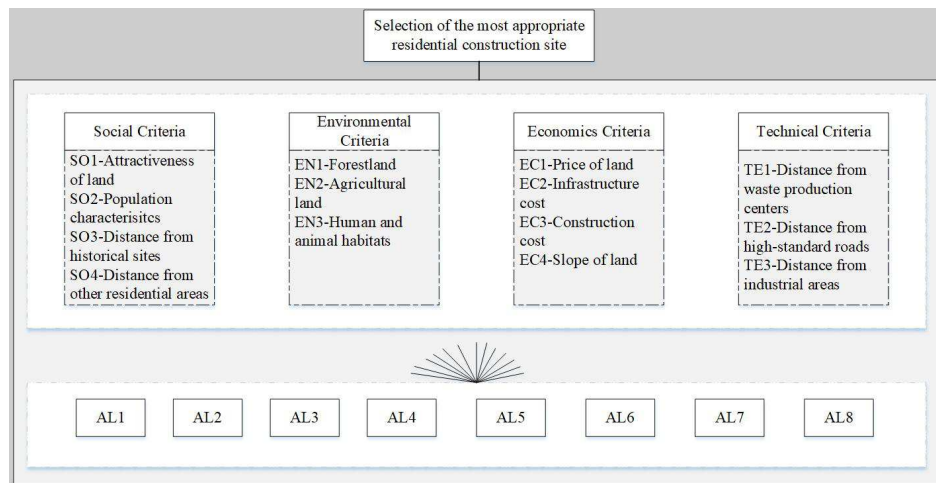


Fig. 3. Hierarchy of the application.

The hierarchy involving the specified criteria and alternatives is given in Fig. 3.

5.2. Solution of Application

As the first step of our proposed hesitant fuzzy CODAS method, the initial decision matrix involving linguistic assessments is constructed in Table 3. In this table, the committee can assign different linguistic evaluations for each criterion. The number of these evaluations may change from one to four since the hesitant fuzzy approach requires it. The hyphens

in the table indicate that a member of the committee did not prefer making an evaluation for the related alternative with respect to the considered criterion.

Secondly, the initial decision matrix is converted to the decision matrix with corresponding numerical membership degrees. The decision matrix is constructed in Table 4. After this point of the method, we partially present the normalized decision matrix (Table 5) and weighted normalized decision matrix (Table 6) because of the space constraints.

As the next step, we calculate the negative-ideal solution by using Eq. (35). The negative solution is found as $(\langle [0.016, 0.032], [0.005, 0.019], [0.005, 0.019], [0.007, 0.026] \rangle, \langle [0.034, 0.06], [0.009, 0.031], [0.012, 0.046], [0.012, 0.046] \rangle, \langle [0.062, 0.111], [0.031, 0.062], [0.026, 0.064], [0.012, 0.043] \rangle, \langle [0.009, 0.018], [0.003, 0.011], [0.003, 0.013], [0.003, 0.013] \rangle, \langle [0.023, 0.023], [0.028, 0.039], [0.023, 0.034], [0.013, 0.02] \rangle, \langle [0.065, 0.092], [0.032, 0.045], [0.021, 0.032], [0.002, 0.003] \rangle, \langle [0.052, 0.071], [0.017, 0.024], [0.024, 0.037], [0.029, 0.052] \rangle, \langle [0.032, 0.044], [0.02, 0.027], [0.011, 0.015], [0.015, 0.023] \rangle, \langle [0.101, 0.152], [0.06, 0.062], [0.033, 0.052], [0.018, 0.021] \rangle, \langle [0.085, 0.12], [0.02, 0.027], [0.023, 0.033], [0.027, 0.043] \rangle, \langle [0.013, 0.019], [0.006, 0.008], [0.012, 0.025], [0.005, 0.009] \rangle, \langle [0.027, 0.041], [0.004, 0.005], [0.004, 0.006], [0.005, 0.007] \rangle, \langle [0.022, 0.032], [0.01, 0.013], [0.006, 0.009], [0.006, 0.009] \rangle, \langle [0.074, 0.105], [0.06, 0.087], [0.017, 0.024], [0.002, 0.002] \rangle).$

Then, Euclidean and Hamming distances to negative-ideal solution are calculated as in Table 7.

At the final step, the relative assessment matrix is constructed, and scores are calculated (see Table 8).

The results indicate that AL4 is the best alternative for construction site. The ranking of alternative sites is as follows: $AL4 > AL1 > AL3 > AL8 > AL5 > AL6 > AL7 > AL2$.

5.3. Comparison with Ordinary Fuzzy CODAS and Hesitant TOPSIS Methods

In this sub-section, we compare our novel hesitant CODAS method with the ordinary fuzzy CODAS method. The membership values in the decision matrix of hesitant fuzzy CODAS are aggregated and thus, unified interval-valued fuzzy numbers are obtained to apply ordinary fuzzy CODAS method. Since trapezoidal fuzzy numbers are used in ordinary fuzzy CODAS method proposed by Keshavarz Ghorabae *et al.* (2017), interval-valued fuzzy numbers are converted to trapezoidal fuzzy numbers. For instance, (3.15, 4.95) is converted to (3.15, 3.15, 4.95, 4.95). The aggregated decision matrix is given in Table 9.

The results of the ordinary fuzzy CODAS method are given in Table 10.

We apply different decision matrices since the different rankings are obtained from the ordinary fuzzy CODAS method. In most of the cases, both methods produced the same results. However, when the fuzziness is increased, our proposed method overcomes the disadvantages of the ordinary fuzzy sets and gives better solutions than the ordinary fuzzy CODAS method.

Secondly, we also compare our proposed method with hesitant fuzzy TOPSIS (Xu and Zhang, 2013). We used the same weighted normalized decision matrix since both methods

Table 3
Decision matrix with linguistic terms.

	SO1			SO2			SO3			SO4			EN1			EN2			EN3									
AL1	MG	VP	-	VG	MG	-	F	MG	MG	G	MG	MG	VG	-	MG	F	F	G	F	F	F	P	-	VP	P	MP	VP	VP
AL2	-	MP	VP	VP	VG	MP	-	MG	G	MP	F	VG	F	G	G	MP	-	F	-	MP	UI	F	VG	G	F	MG	G	MP
AL3	P	VG	MP	F	F	MG	G	-	VG	MP	-	P	-	MP	VP	-	P	MG	-	G	-	VP	MP	MG	G	MP	MP	F
AL4	P	VG	-	VP	MG	-	F	VG	VG	F	MG	VG	-	G	VG	MG	VP	P	G	G	MG	-	VG	F	P	VG	MP	G
AL5	VG	MG	SP	VG	G	F	MP	SP	G	VP	F	P	MG	-	VG	VP	MP	VP	G	MG	MP	VG	MG	MP	-	P	G	F
AL6	VG	VP	G	P	MG	F	G	MP	MG	F	MP	P	-	G	G	MP	VG	F	VG	MG	MG	VG	MP	MP	-	-	VP	MG
AL7	MG	P	F	VG	F	VG	MP	G	-	G	G	P	VG	VP	MG	MG	F	G	F	MP	P	MP	MG	F	VP	VP	G	P
AL8	F	VP	F	-	F	VP	-	VP	P	P	G	VG	MG	VG	F	VP	MG	-	P	MP	VG	-	F	G	P	P	G	G
	EC1			EC2			EC3			EC4			TE1			TE2			TE3									
AL1	P	VP	-	F	MG	-	G	F	P	G	MP	P	P	VG	MG	P	G	VG	VP	VG	VG	-	-	MG	G	VP	MG	UI
AL2	MP	MG	P	MG	G	G	MG	VG	MP	MP	F	VG	MG	MP	G	MP	VP	VP	MG	P	P	VG	P	-	-	VG	G	-
AL3	G	G	MP	VG	F	G	MP	F	VP	G	G	MG	VG	P	VG	P	MG	P	VP	MG	MG	VP	F	VP	MP	G	-	VP
AL4	MP	P	-	G	VP	P	VG	MG	F	-	F	MG	MP	-	P	G	VP	VP	MG	MP	MP	VP	MP	F	F	P	P	MP
AL5	P	MP	-	P	MP	MG	-	G	F	F	F	MG	F	MP	P	F	G	MG	VG	G	F	MG	G	F	MP	MP	VP	G
AL6	VP	VG	F	MP	MP	G	F	-	VP	-	F	-	VG	P	P	-	MG	G	MG	F	VG	MG	VP	MP	VP	F	MP	G
AL7	VG	MG	F	VG	P	MG	-	MP	P	VG	F	P	MP	-	F	P	VG	P	-	P	MP	VG	VG	P	G	MP	G	MP
AL8	P	G	-	-	VG	VP	F	G	MG	MP	F	VP	MG	VP	VG	P	VP	G	-	VP	VG	F	MP	G	UI	VP	VG	G

Table 4
Decision matrix with membership degrees.

BENEFFT				BENEFFT				BENEFFT				BENEFFT				COST				COST				COST							
0.0464				0.0680				0.0783				0.0227				0.0702				0.1140				0.1316							
SO1				SO2				SO3				SO4				EN1				EN2				EN3							
MS1	MS2	MS3	MS4	MS1	MS2	MS3	MS4	MS1	MS2	MS3	MS4	MS1	MS2	MS3	MS4	MS1	MS2	MS3	MS4	MS1	MS2	MS3	MS4	MS1	MS2	MS3	MS4				
AL1	[6.3, 8.1]	[4.5, 6.3]	[0.9, 2.7]	[0.9, 2.7]	[4.5, 6.3]	[4.5, 6.3]	[3.6, 5.4]	[3.6, 5.4]	[5.4, 7.2]	[4.5, 6.3]	[4.5, 6.3]	[4.5, 6.3]	[6.3, 8.1]	[4.5, 6.3]	[3.6, 5.4]	[3.6, 5.4]	[3.6, 5.4]	[3.6, 5.4]	[3.6, 5.4]	[3.6, 5.4]	[3.6, 5.4]	[1.8, 3.6]	[0.9, 2.7]	[0.9, 2.7]	[2.7, 4.5]	[1.8, 3.6]	[0.9, 2.7]	[0.9, 2.7]			
AL2	[2.7, 4.5]	[0.9, 2.7]	[0.9, 2.7]	[0.9, 2.7]	[6.3, 8.1]	[4.5, 6.3]	[2.7, 4.5]	[2.7, 4.5]	[6.3, 8.1]	[5.4, 7.2]	[3.6, 5.4]	[2.7, 4.5]	[5.4, 7.2]	[5.4, 7.2]	[3.6, 5.4]	[2.7, 4.5]	[2.7, 4.5]	[2.7, 4.5]	[2.7, 4.5]	[2.7, 4.5]	[6.3, 8.1]	[5.4, 7.2]	[3.6, 5.4]	[0.1, 1.8]	[5.4, 7.2]	[4.5, 6.3]	[3.6, 5.4]	[2.7, 4.5]			
AL3	[6.3, 8.1]	[3.6, 5.4]	[2.7, 4.5]	[1.8, 3.6]	[5.4, 7.2]	[4.5, 6.3]	[3.6, 5.4]	[3.6, 5.4]	[6.3, 8.1]	[2.7, 4.5]	[1.8, 3.6]	[1.8, 3.6]	[2.7, 4.5]	[0.9, 2.7]	[0.9, 2.7]	[0.9, 2.7]	[1.8, 3.6]	[4.5, 6.3]	[1.8, 3.6]	[4.5, 6.3]	[2.7, 4.5]	[0.9, 2.7]	[0.9, 2.7]	[5.4, 7.2]	[3.6, 5.4]	[2.7, 4.5]	[2.7, 4.5]				
AL4	[6.3, 8.1]	[1.8, 3.6]	[0.9, 2.7]	[0.9, 2.7]	[6.3, 8.1]	[4.5, 6.3]	[3.6, 5.4]	[3.6, 5.4]	[6.3, 8.1]	[6.3, 8.1]	[4.5, 6.3]	[3.6, 5.4]	[6.3, 8.1]	[5.4, 7.2]	[4.5, 6.3]	[4.5, 6.3]	[4.5, 6.3]	[5.4, 7.2]	[5.4, 7.2]	[1.8, 3.6]	[0.9, 2.7]	[6.3, 8.1]	[4.5, 6.3]	[3.6, 5.4]	[6.3, 8.1]	[5.4, 7.2]	[2.7, 4.5]	[1.8, 3.6]			
AL5	[7.2, 9]	[6.3, 8.1]	[6.3, 8.1]	[4.5, 6.3]	[7.2, 9]	[5.4, 7.2]	[3.6, 5.4]	[2.7, 4.5]	[5.4, 7.2]	[3.6, 5.4]	[1.8, 3.6]	[0.9, 2.7]	[6.3, 8.1]	[4.5, 6.3]	[0.9, 2.7]	[0.9, 2.7]	[2.7, 6.3]	[4.5, 6.3]	[2.7, 4.5]	[0.9, 2.7]	[6.3, 8.1]	[4.5, 6.3]	[2.7, 4.5]	[2.7, 4.5]	[5.4, 7.2]	[3.6, 5.4]	[1.8, 3.6]	[1.8, 3.6]			
AL6	[6.3, 8.1]	[5.4, 6.3]	[1.8, 3.6]	[0.9, 2.7]	[5.4, 7.2]	[4.5, 6.3]	[3.6, 4.5]	[2.7, 4.5]	[4.5, 6.3]	[3.6, 5.4]	[2.7, 4.5]	[1.8, 3.6]	[5.4, 7.2]	[5.4, 7.2]	[2.7, 4.5]	[2.7, 4.5]	[6.3, 8.1]	[6.3, 8.1]	[4.6, 6.3]	[3.6, 5.4]	[6.3, 8.1]	[4.5, 6.3]	[2.7, 4.5]	[2.7, 4.5]	[4.5, 6.3]	[0.9, 2.7]	[0.9, 2.7]	[0.9, 2.7]			
AL7	[6.3, 8.1]	[5.4, 6.3]	[4.5, 6.3]	[1.8, 3.6]	[6.3, 8.1]	[5.4, 7.2]	[4.5, 5.4]	[3.6, 5.4]	[5.4, 7.2]	[5.4, 7.2]	[1.8, 3.6]	[1.8, 3.6]	[6.3, 8.1]	[4.5, 6.3]	[4.5, 6.3]	[0.9, 2.7]	[3.6, 5.4]	[3.6, 5.4]	[3.6, 5.4]	[2.7, 4.5]	[4.5, 6.3]	[3.6, 5.4]	[2.7, 4.5]	[1.8, 3.6]	[5.4, 7.2]	[1.8, 3.6]	[0.9, 2.7]	[0.9, 2.7]			
AL8	[3.6, 5.4]	[3.6, 5.4]	[0.9, 2.7]	[0.9, 2.7]	[3.6, 5.4]	[0.9, 2.7]	[0.9, 2.7]	[0.9, 2.7]	[6.3, 8.1]	[5.4, 7.2]	[1.8, 3.6]	[1.8, 3.6]	[6.3, 8.1]	[4.5, 6.3]	[3.6, 5.4]	[0.9, 2.7]	[2.7, 3.6]	[2.7, 4.5]	[1.8, 3.6]	[1.8, 3.6]	[6.3, 8.1]	[5.4, 7.2]	[3.6, 5.4]	[3.6, 5.4]	[5.4, 7.2]	[5.4, 7.2]	[1.8, 3.6]	[1.8, 3.6]			
COST				COST				COST				COST				BENEFFT				COST				COST							
0.0808				0.1313				0.1515				0.0227				0.0332				0.0383				0.1313							
EC1				EC2				EC3				EC4				TE1				TE2				TE3							
MS1	MS2	MS3	MS4	MS1	MS2	MS3	MS4	MS1	MS2	MS3	MS4	MS1	MS2	MS3	MS4	MS1	MS2	MS3	MS4	MS1	MS2	MS3	MS4	MS1	MS2	MS3	MS4	MS1	MS2	MS3	MS4
AL1	[3.6, 5.4]	[1.8, 3.6]	[0.9, 2.7]	[0.9, 2.7]	[5.4, 7.2]	[5.4, 5.4]	[3.6, 4.5]	[3.6, 4.5]	[5.4, 7.2]	[2.7, 4.5]	[1.8, 3.6]	[1.8, 3.6]	[6.3, 8.1]	[4.5, 6.3]	[1.8, 3.6]	[1.8, 3.6]	[6.3, 8.1]	[6.3, 8.1]	[5.4, 7.2]	[0.9, 2.7]	[6.3, 8.1]	[4.5, 6.3]	[4.5, 6.3]	[4.5, 6.3]	[5.4, 7.2]	[4.5, 6.3]	[0.9, 2.7]	[0.1, 1.8]			
AL2	[4.5, 6.3]	[4.5, 6.3]	[2.7, 4.5]	[1.8, 3.6]	[6.3, 8.1]	[7.2, 9]	[5.4, 8.1]	[6.7]	[6.3, 8.1]	[3.6, 5.4]	[2.7, 4.5]	[2.7, 4.5]	[5.4, 7.2]	[4.5, 6.3]	[2.7, 4.5]	[2.7, 4.5]	[4.5, 6.3]	[2.7, 4.5]	[1.8, 3.6]	[0.9, 2.7]	[6.3, 8.1]	[1.8, 3.6]	[1.8, 3.6]	[1.8, 3.6]	[6.3, 8.1]	[5.4, 7.2]	[5.4, 7.2]	[5.4, 7.2]			
AL3	[6.3, 8.1]	[5.4, 7.2]	[5.4, 7.2]	[2.7, 4.5]	[5.4, 7.2]	[3.6, 5.4]	[3.6, 5.4]	[2.7, 4.5]	[5.4, 7.2]	[5.4, 7.2]	[4.5, 6.3]	[0.9, 2.7]	[6.3, 8.1]	[6.3, 8.1]	[1.8, 3.6]	[1.8, 3.6]	[4.5, 6.3]	[4.5, 6.3]	[1.8, 3.6]	[0.9, 2.7]	[4.5, 6.3]	[3.6, 5.4]	[0.9, 2.7]	[5.4, 7.2]	[2.7, 4.5]	[0.9, 2.7]	[0.9, 2.7]				
AL4	[5.4, 7.2]	[3.6, 4.5]	[1.8, 2.7]	[1.8, 2.7]	[6.3, 8.1]	[4.5, 6.3]	[1.8, 3.6]	[0.9, 2.7]	[4.5, 6.3]	[3.6, 5.4]	[3.6, 5.4]	[3.6, 5.4]	[5.4, 7.2]	[2.7, 4.5]	[1.8, 3.6]	[1.8, 3.6]	[4.5, 6.3]	[2.7, 4.5]	[2.7, 4.5]	[0.9, 2.7]	[3.6, 5.4]	[2.7, 4.5]	[2.7, 4.5]	[2.7, 4.5]	[0.9, 2.7]	[3.6, 5.4]	[1.8, 3.6]	[1.8, 3.6]			
AL5	[2.7, 4.5]	[1.8, 3.6]	[1.8, 3.6]	[1.8, 3.6]	[5.4, 7.2]	[4.5, 6.3]	[2.7, 4.5]	[2.7, 4.5]	[4.5, 6.3]	[3.6, 5.4]	[3.6, 5.4]	[3.6, 5.4]	[3.6, 5.4]	[3.6, 5.4]	[2.7, 4.5]	[1.8, 3.6]	[6.3, 8.1]	[5.4, 7.2]	[5.4, 7.2]	[4.5, 6.3]	[5.4, 7.2]	[4.5, 6.3]	[3.6, 5.4]	[3.6, 5.4]	[5.4, 7.2]	[2.7, 4.5]	[2.7, 4.5]	[1.8, 3.6]			
AL6	[6.3, 8.1]	[3.6, 5.4]	[2.7, 4.5]	[0.9, 2.7]	[5.4, 7.2]	[3.6, 5.4]	[2.7, 4.5]	[2.7, 4.5]	[3.6, 5.4]	[0.9, 2.7]	[0.9, 2.7]	[0.9, 2.7]	[6.3, 8.1]	[1.8, 3.6]	[1.8, 3.6]	[1.8, 3.6]	[1.8, 3.6]	[5.4, 7.2]	[4.5, 6.3]	[3.6, 5.4]	[6.3, 8.1]	[4.5, 6.3]	[2.7, 4.5]	[0.9, 2.7]	[5.4, 7.2]	[3.6, 5.4]	[2.7, 4.5]	[0.9, 2.7]			
AL7	[6.3, 8.1]	[6.3, 8.1]	[4.5, 6.3]	[3.6, 5.4]	[4.5, 6.3]	[2.7, 4.5]	[1.8, 3.6]	[1.8, 3.6]	[6.3, 8.1]	[3.6, 5.4]	[1.8, 3.6]	[1.8, 3.6]	[6.3, 8.1]	[2.7, 4.5]	[1.8, 3.6]	[1.8, 3.6]	[6.3, 8.1]	[1.8, 3.6]	[1.8, 3.6]	[1.8, 3.6]	[6.3, 8.1]	[6.3, 8.1]	[2.7, 4.5]	[1.8, 3.6]	[5.4, 7.2]	[2.7, 4.5]	[2.7, 4.5]	[2.7, 4.5]			
AL8	[5.4, 7.2]	[1.8, 3.6]	[1.8, 3.6]	[1.8, 3.6]	[6.3, 8.1]	[5.4, 7.2]	[3.6, 5.4]	[0.9, 2.7]	[4.5, 6.3]	[3.6, 5.4]	[2.7, 3.6]	[0.9, 2.7]	[6.3, 8.1]	[4.5, 6.3]	[1.8, 3.6]	[0.9, 2.7]	[5.4, 7.2]	[0.9, 2.7]	[0.9, 2.7]	[0.9, 2.7]	[6.3, 8.1]	[5.4, 7.2]	[3.6, 5.4]	[2.7, 4.5]	[6.3, 8.1]	[5.4, 7.2]	[0.9, 2.7]	[0.1, 1.8]			

Table 5
Normalized decision matrix.

Type	BENEFIT				COST			
Weight	0.0464				0.1313			
Criteria	SO1				TE3			
Membership	MS1	MS2	MS3	MS4	MS1	MS2	MS3	MS4
AL1	[0.7, 0.9]	[0.56, 0.78]	[0.11, 0.33]	[0.14, 0.43]	[0.5, 0.67]	[0.43, 0.6]	[0.33, 1]	[0.06, 1]
AL2	[0.3, 0.5]	[0.11, 0.33]	[0.11, 0.33]	[0.14, 0.43]	[0.44, 0.57]	[0.38, 0.5]	[0.13, 0.17]	[0.01, 0.02]
AL3	[0.7, 0.9]	[0.44, 0.67]	[0.33, 0.56]	[0.29, 0.57]	[0.5, 0.67]	[0.6, 1]	[0.33, 1]	[0.04, 0.11]
AL4	[0.7, 0.9]	[0.22, 0.44]	[0.11, 0.33]	[0.14, 0.43]	[0.67, 1]	[0.6, 1]	[0.25, 0.5]	[0.03, 0.06]
AL5	[0.8, 1]	[0.78, 1]	[0.78, 1]	[0.71, 1]	[0.5, 0.67]	[0.6, 1]	[0.2, 0.33]	[0.03, 0.06]
AL6	[0.7, 0.9]	[0.67, 0.78]	[0.22, 0.44]	[0.14, 0.43]	[0.5, 0.67]	[0.5, 0.75]	[0.2, 0.33]	[0.04, 0.11]
AL7	[0.7, 0.9]	[0.67, 0.78]	[0.56, 0.78]	[0.29, 0.57]	[0.5, 0.67]	[0.38, 0.5]	[0.2, 0.33]	[0.02, 0.04]
AL8	[0.4, 0.6]	[0.44, 0.67]	[0.11, 0.33]	[0.14, 0.43]	[0.44, 0.57]	[0.38, 0.5]	[0.33, 1]	[0.06, 1]

Table 6
Weighted normalized decision matrix.

Type	BENEFIT				COST			
Weight	0.0464				0.1313			
Criteria	SO1				TE3			
Membership	MS1	MS2	MS3	MS4	MS1	MS2	MS3	MS4
AL1	[0.054, 0.101]	[0.037, 0.067]	[0.005, 0.019]	[0.007, 0.026]	[0.052, 1]	[0.052, 1]	[0.054, 0.106]	[0.054, 1]
AL2	[0.016, 0.032]	[0.005, 0.019]	[0.005, 0.019]	[0.007, 0.026]	[0.024, 0.037]	[0.029, 0.052]	[0.044, 0.071]	[0.027, 0.04]
AL3	[0.054, 0.101]	[0.027, 0.05]	[0.019, 0.037]	[0.015, 0.039]	[0.029, 0.052]	[0.029, 0.052]	[0.032, 0.044]	[0.023, 0.032]
AL4	[0.054, 0.101]	[0.012, 0.027]	[0.005, 0.019]	[0.007, 0.026]	[0.029, 0.052]	[0.037, 0.087]	[0.037, 0.054]	[0.04, 0.054]
AL5	[0.072, 1]	[0.067, 1]	[0.067, 1]	[0.056, 1]	[0.037, 0.087]	[0.037, 0.087]	[0.071, 1]	[0.054, 1]
AL6	[0.054, 0.101]	[0.05, 0.067]	[0.012, 0.027]	[0.007, 0.026]	[0.052, 1]	[0.052, 1]	[0.032, 0.044]	[0.032, 0.054]
AL7	[0.054, 0.101]	[0.05, 0.067]	[0.037, 0.067]	[0.015, 0.039]	[0.052, 1]	[0.052, 1]	[0.032, 0.044]	[0.02, 0.027]
AL8	[0.023, 0.042]	[0.027, 0.05]	[0.005, 0.019]	[0.007, 0.026]	[0.037, 0.087]	[0.037, 0.087]	[0.037, 0.054]	[0.054, 1]

Table 7
Euclidean and Hamming distances to negative-ideal solution.

	SO1	SO2	SO3	SO4	EN1	EN2	EN3	EC1	EC2	EC3	EC4	TE1	TE2	TE3	
Euclidean distance	AL1	0.0347	0.4797	0.4755	0.3479	0.0242	0.5786	0.5808	0.5999	0.0311	0.0367	0.3449	0.3510	0.0026	0.4939
	AL2	0.0000	0.0652	0.3193	0.3504	0.3414	0.3524	0.0067	0.0178	0.0000	0.0133	0.0026	0.4881	0.3492	0.0000
	AL3	0.0325	0.4800	0.3149	0.0000	0.5961	0.3445	0.0100	0.0041	0.0475	0.3389	0.3449	0.4881	0.4959	0.4733
	AL4	0.0283	0.4808	0.5671	0.6978	0.4866	0.0045	0.0139	0.0241	0.4827	0.0368	0.3449	0.4881	0.4901	0.4535
	AL5	0.6916	0.5865	0.0202	0.3475	0.3479	0.0066	0.0238	0.4830	0.0439	0.0368	0.3469	0.0004	0.0046	0.3237
	AL6	0.0366	0.0611	0.0174	0.3503	0.0000	0.0066	0.5899	0.3457	0.0551	0.6689	0.4920	0.0065	0.3506	0.0338
	AL7	0.0421	0.5903	0.0436	0.4927	0.0244	0.0312	0.4785	0.0013	0.5603	0.0327	0.4892	0.0106	0.0070	0.0156
	AL8	0.0140	0.0000	0.3173	0.3477	0.4828	0.0000	0.0232	0.3448	0.3467	0.3408	0.4916	0.6086	0.0030	0.4937
Hamming distance	AL1	0.1532	0.5260	0.5232	0.3796	0.1322	0.6087	0.6160	0.6218	0.1673	0.1773	0.3524	0.3537	0.0350	0.5115
	AL2	0.0000	0.2474	0.4005	0.3764	0.3808	0.3538	0.0633	0.1245	0.0000	0.1013	0.0415	0.5010	0.3622	0.0000
	AL3	0.1631	0.5306	0.3489	0.0000	0.6136	0.3880	0.0894	0.0510	0.1953	0.3600	0.3513	0.4999	0.5073	0.5044
	AL4	0.1234	0.5376	0.6236	0.7113	0.5028	0.0458	0.0891	0.1474	0.5096	0.1446	0.3567	0.4995	0.5044	0.5014
	AL5	0.7189	0.6299	0.1132	0.3641	0.3846	0.0668	0.1373	0.5117	0.1925	0.1446	0.3556	0.0135	0.0613	0.3631
	AL6	0.1639	0.2388	0.1204	0.3729	0.0000	0.0668	0.6159	0.3639	0.2138	0.7029	0.4989	0.0623	0.3571	0.1597
	AL7	0.1943	0.6372	0.1771	0.5090	0.1373	0.1451	0.5086	0.0247	0.6101	0.1505	0.5003	0.0901	0.0635	0.1031
	AL8	0.0932	0.0000	0.3744	0.3719	0.5150	0.0000	0.1280	0.3733	0.3694	0.3856	0.4975	0.6155	0.0461	0.5017

have the same steps to obtain it. The positive ideal solutions of hesitant TOPSIS method are given in Table 11.

The negative ideal solutions of the hesitant TOPSIS method are given in Table 12.

After the calculations, results of the hesitant TOPSIS method are calculated as in Table 13.

The results of the compared methods are the same. Thus, our proposed model is valid where hesitant fuzzy sets can be used as input data.

Table 8
Relative assessment matrix and assessment scores based on HF-CODAS.

	AL1	AL2	AL3	AL4	AL5	AL6	AL7	AL8	Scores	Rank
AL1	0	4.28	0.97	-0.36	2.22	2.59	2.87	1.45	14	2
AL2	-4.28	0	-3.31	-4.64	-2.06	-1.69	-1.41	-2.83	-20.2	8
AL3	-0.97	3.31	0	-1.32	1.25	1.62	1.9	0.49	6.29	3
AL4	0.36	4.64	1.32	0	2.58	2.94	3.23	1.81	16.9	1
AL5	-2.22	2.06	-1.25	-2.58	0	0.37	0.65	-0.77	-3.73	5
AL6	-2.59	1.69	-1.62	-2.94	-0.37	0	0.28	-1.13	-6.68	6
AL7	-2.87	1.41	-1.9	-3.23	-0.65	-0.28	0	-1.42	-8.93	7
AL8	-1.45	2.83	-0.49	-1.81	0.77	1.13	1.42	0	2.39	4

Table 9
Decision matrix of ordinary fuzzy CODAS.

	SO1	SO2	SO3	SO4	EN1	EN2	EN3
AL1	(3.15, 4.95)	(4.05, 5.85)	(4.73, 6.53)	(4.5, 6.3)	(3.6, 5.4)	(1.8, 3.6)	(1.58, 3.38)
AL2	(1.35, 3.15)	(4.05, 5.85)	(4.5, 6.3)	(4.28, 6.08)	(2.7, 4.5)	(3.85, 5.63)	(4.05, 5.85)
AL3	(3.6, 5.4)	(4.28, 6.08)	(3.15, 4.95)	(1.35, 3.15)	(2.48, 4.95)	(2.25, 4.05)	(3.6, 5.4)
AL4	(2.48, 4.28)	(4.5, 6.3)	(5.18, 6.98)	(5.18, 6.98)	(3.15, 5.18)	(4.5, 6.3)	(4.05, 5.85)
AL5	(6.08, 7.88)	(4.73, 6.53)	(2.93, 4.73)	(3.15, 4.95)	(2.7, 4.95)	(4.05, 5.85)	(3.15, 4.95)
AL6	(3.6, 5.18)	(4.05, 5.63)	(3.15, 4.95)	(4.05, 5.85)	(5.2, 6.98)	(4.05, 5.85)	(1.8, 3.6)
AL7	(4.5, 6.08)	(4.95, 6.53)	(3.6, 5.4)	(4.05, 5.85)	(3.38, 5.18)	(3.15, 4.95)	(2.25, 4.05)
AL8	(2.25, 4.05)	(1.58, 3.38)	(3.83, 5.63)	(3.83, 5.63)	(2.25, 3.83)	(4.73, 6.53)	(3.6, 5.4)
	EC1	EC2	EC3	EC4	TE1	TE2	TE3
AL1	(1.8, 3.6)	(4.5, 5.4)	(2.93, 4.73)	(3.6, 5.4)	(4.73, 6.53)	(4.95, 6.75)	(2.73, 4.5)
AL2	(3.38, 5.18)	(6.18, 7.58)	(3.83, 5.63)	(3.83, 5.63)	(2.48, 4.28)	(2.93, 4.73)	(5.63, 7.43)
AL3	(4.95, 6.75)	(3.83, 5.63)	(4.05, 5.85)	(4.05, 5.85)	(2.93, 4.73)	(2.48, 4.28)	(2.48, 4.28)
AL4	(3.15, 4.28)	(3.38, 5.18)	(3.83, 5.63)	(2.93, 4.73)	(2.7, 4.5)	(2.48, 4.28)	(2.48, 4.28)
AL5	(2.03, 3.83)	(3.83, 5.63)	(3.83, 5.63)	(2.93, 4.73)	(5.4, 7.2)	(4.28, 6.08)	(3.15, 4.95)
AL6	(3.38, 5.18)	(3.6, 5.4)	(1.58, 3.38)	(2.93, 4.58)	(4.5, 6.3)	(3.6, 5.4)	(3.15, 4.95)
AL7	(5.18, 6.98)	(2.7, 4.5)	(3.38, 5.18)	(2.48, 4.28)	(2.93, 4.73)	(4.28, 6.08)	(4.05, 5.85)
AL8	(2.7, 4.5)	(4.05, 5.85)	(2.93, 4.5)	(3.38, 5.18)	(2.03, 3.83)	(4.5, 6.3)	(3.18, 4.95)

Table 10
Relative assessment matrix and assessment scores for ordinary fuzzy CODAS method.

	AL1	AL2	AL3	AL4	AL5	AL6	AL7	AL8	Scores	Rank
AL1	0.00	0.36	0.19	0.18	0.18	0.11	0.18	0.29	1.49	1
AL2	-0.36	0.00	-0.17	-0.18	-0.18	-0.25	-0.18	-0.08	-1.41	8
AL3	-0.19	0.17	0.00	0.00	-0.01	-0.08	0.00	0.10	-0.01	6
AL4	-0.18	0.18	0.00	0.00	0.00	-0.07	0.00	0.10	0.02	5
AL5	-0.18	0.18	0.01	0.00	0.00	-0.07	0.00	0.11	0.06	3
AL6	-0.11	0.25	0.08	0.07	0.07	0.00	0.07	0.17	0.59	2
AL7	-0.18	0.18	0.00	0.00	0.00	-0.07	0.00	0.11	0.05	4
AL8	-0.29	0.08	-0.10	-0.10	-0.11	-0.17	-0.11	0.00	-0.80	7

5.4. Sensitivity Analysis

One-at-a-time sensitivity analysis based on each criterion is performed to demonstrate the effects of changes on the results. To visualize this analysis, we develop a pattern which is

Table 11
Positive ideal solutions of hesitant TOPSIS method.

	SO1	SO2	SO3	SO4	EN1	EN2	EN3	EC1	EC2	EC3	EC4	TE1	TE2	TE3	Sum
AL1	0.671	0.448	0.433	0.585	0.674	0.349	0.323	0.316	0.63	0.635	0.603	0.602	0.695	0.494	7.46
AL2	0.692	0.618	0.533	0.588	0.577	0.579	0.672	0.672	0.658	0.658	0.695	0.491	0.595	0.704	8.73
AL3	0.668	0.442	0.575	0.698	0.473	0.553	0.667	0.686	0.618	0.57	0.604	0.492	0.479	0.497	8.02
AL4	0.678	0.431	0.304	0	0.479	0.675	0.667	0.669	0.434	0.649	0.599	0.493	0.486	0.498	7.06
AL5	0	0.313	0.648	0.598	0.569	0.673	0.655	0.473	0.619	0.649	0.601	0.697	0.693	0.609	7.8
AL6	0.669	0.625	0.646	0.591	0.687	0.673	0.314	0.586	0.609	0	0.491	0.693	0.599	0.701	7.88
AL7	0.659	0.302	0.63	0.485	0.669	0.656	0.457	0.688	0.323	0.644	0.49	0.688	0.692	0.703	8.09
AL8	0.684	0.677	0.556	0.592	0.47	0.677	0.657	0.579	0.547	0.55	0.492	0.333	0.694	0.496	8

Table 12
Positive ideal solution of hesitant TOPSIS method.

	SO1	SO2	SO3	SO4	EN1	EN2	EN3	EC1	EC2	EC3	EC4	TE1	TE2	TE3	Sum
AL1	0.035	0.48	0.476	0.348	0.021	0.579	0.581	0.6	0.032	0.037	0.345	0.351	0.003	0.499	4.39
AL2	0	0.065	0.319	0.35	0.341	0.352	0.007	0.018	0	0.013	0.003	0.488	0.349	0	2.31
AL3	0.032	0.48	0.315	0	0.486	0.345	0.01	0.004	0.048	0.339	0.345	0.488	0.496	0.498	3.88
AL4	0.028	0.481	0.567	0.698	0.487	0.004	0.014	0.024	0.483	0.037	0.345	0.488	0.49	0.496	4.64
AL5	0.692	0.586	0.02	0.348	0.347	0.007	0.024	0.483	0.044	0.037	0.347	0.0004	0.005	0.351	3.29
AL6	0.037	0.061	0.017	0.35	0	0.007	0.59	0.346	0.055	0.669	0.492	0.006	0.351	0.003	2.98
AL7	0.042	0.59	0.044	0.493	0.023	0.031	0.479	0.001	0.56	0.033	0.489	0.011	0.007	0.001	2.8
AL8	0.014	0	0.317	0.348	0.483	0	0.023	0.345	0.347	0.341	0.492	0.609	0.003	0.499	3.82

Table 13
Positive ideal solution of hesitant TOPSIS method.

	AL1	AL2	AL3	AL4	AL5	AL6	AL7	AL8
Score	0.37	0.21	0.33	0.4	0.3	0.27	0.26	0.32
Rank	2	8	3	1	5	6	7	4

Table 14
Pattern for the sensitivity analysis.

Pattern	Sets with respect to criteria		
	SO1	SO2	TE3
Test variables			
0.1	AL4, AL1	AL4, AL1	AL4, AL1
0.2	AL4, AL1	AL4, AL1	AL4, AL1
0.3	AL4, AL1	AL4, AL1	AL4, AL1
0.4	AL4, AL1	AL4, AL1	AL4, AL1
0.5	AL4, AL1	AL4, AL1	AL4, AL1
0.6	AL4, AL1	AL4, AL1	AL4, AL1
0.7	AL4, AL1	AL4, AL1	AL4, AL1
0.8	AL4, AL1	AL4, AL1	AL4, AL1
0.9	AL4, AL1	AL4, AL1	AL4, AL1
1.0	AL4, AL1	AL4, AL1	AL4, AL1

given in Table 14. After the changes on weights of the sub-criteria through this pattern, hesitant fuzzy CODAS method operations are re-processed. In Table 14, only the first and second alternatives are presented.

When the results of the sensitivity analyses are examined, it is revealed that criterion SO2 with an interval of [0.7, 1] and criterion EC3 with an interval of [0.7, 1] affect the results. But they don't affect the rank of the best alternative. This verifies the robustness of the proposed model on the given decision.

6. Conclusions

In today's world, urban cities are getting larger and many residential areas are constructed to supply the demand of housing needs. Residential construction site selection problem is an MCDM problem since it includes many alternatives and criteria which might be tangible and intangible. This study has developed a new hesitant fuzzy MCDM extension of CODAS method aiming at selecting the most suitable construction site location. CODAS method is a useful and efficient distance-based method since it combines the advantages of Euclidean and Hamming distances. It has been applied to the selection problem of the best location site of a residential site in Istanbul. Sensitivity and comparative analyses have been also realized in order to observe the robustness and sensitiveness of the given decisions.

For further research, considered criteria can be extended by adding the citizen opinions and different user sentiments such as social media networks can be included for the assessment process as such studies (Morente-Molinera *et al.*, 2019). Also, we suggest other fuzzy extensions of CODAS method to be developed for comparative purposes. Neutrosophic CODAS method or Pythagorean fuzzy CODAS method are the possible extensions to develop. Types of fuzzy numbers can be also changed in order to obtain the variants of the developed new extensions. Hesitant fuzzy CODAS can be worked with triangular fuzzy numbers, for instance.

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